

FIGURE 5-12

A B-spline of order 2, called the "hat" function

This makes the computation of B-splines very easy. To find the value of a B-spline of order *m* at θ , we just start with order 1 and keep multiplying and adding according to equation 5.14, until we reach order *m*. Furthermore most of the B-spline values will be zero. Here is what we mean:

Suppose it is desired to find a fifth order B-spline at t which is between the third and fourth knots. We want to find

$$B_{5,3}(t), \quad t_3 < t < t_4$$
 (5.15a)

According to equation 5.14, we must compute first

$$B_{4,3}(t), B_{4,4}(t) \tag{5.15b}$$

and for them we need all of the following

$$B_{3,3}(t), B_{3,4}(t), B_{3,5}(t)$$

$$B_{2,3}(t), B_{2,4}(t), B_{2,5}(t), B_{2,6}(t)$$

$$B_{1,3}(t), B_{1,4}(t), B_{1,5}(t), B_{1,6}(t), B_{1,7}(t)$$

(5.15c)

But, an important point for the reader to notice, B-splines are local to the extent that

$$B_{m,j}(\theta) \begin{cases} = 0, \quad \theta \le t_j \\ \neq 0, \quad t_j < \theta < t_{j+m} \\ = 0, \quad \theta \ge t_{j+m} \end{cases}$$
(5.16)

and therefore, for the interval from knot j to knot j + 1, the only B-splines that contribute anything are

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